## 4.3: Expected Value

## Group Activity

## (a) (0) B B B ( $B$

Beginning in October, 2015, Powerball ${ }^{\circledR}$ became an even larger combined large jackpot game and cash game. Every Wednesday and Saturday night at 10:59 p.m. Eastern Time, we draw five white balls out of a drum with 69 balls and one red ball out of a drum with 26 red balls.
Source: http://www.powerball.com/powerball/pb_prizes.asp
Powerball - Prizes and Odds

| Match | Prize | Odds |
| :---: | :---: | :---: |
| (O+ BALI $\quad$ Grand Prize 1 in 292,201,338.00 |  |  |
|  | \$1,000,000 | 1 in 11,688,053.52 |
|  | \$50,000 | 1 in 913,129.18 |
|  | \$100 | 1 in 36,525.17 |
|  | \$100 | 1 in 14,494.11 |
|  | \$7 | 1 in 579.76 |
|  | \$7 | 1 in 701.33 |
|  | \$4 | 1 in 91.98 |
| 3ALI | \$4 | 1 in 38.32 |
| The overall odds of winning a prize are 1 in 24.87 . <br> The odds presented here are based on a $\$ 2$ play (rounded to two decimal places). |  |  |

1.a. If the current Powerball grand prize amount is $\$ 90$ million, calculate the expected winnings per ticket:
b. Calculate the expected profit or loss for the ticket-holder per Powerball ticket:
2. a. Calculate the expected value of the Subway prize wheel from activity 7A,B. Let's say the mystery prize is a $\$ 20$ gift card.

|  | Sub | Drink | Cookies | Chips | BOGO | Mystery <br> Prize |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Prize <br> Value | $\$ 4.25$ | $\$ 1.60$ | $\$ 1.30$ | $\$ 0.99$ | $\$ 4.25$ |  |
| Probability | $\frac{2}{13}$ | $\frac{2}{13}$ | $\frac{2}{13}$ | $\frac{4}{13}$ | $\frac{2}{13}$ | $\frac{1}{13}$ |


b. What does the expected value mean in this example? Explain it in a complete sentence.
3. Based on historical data, an auto insurance company estimates that a particular customer has a $1.5 \%$ likelihood of having an accident in the next year, with the average insurance payout being $\$ 10,000$.

If the company charges this customer an annual premium of $\$ 500$, what is the company's expected value of this insurance policy?
a. Make a probability table.

| Possibilities | Accident | No <br> Accident |
| :---: | :---: | :---: |
| Payout |  |  |
| Probability |  |  |

b. Calculate the expected value for the company.
4. A company estimates that $7 \%$ of their products will fail after the original warranty period but within 2 years of the purchase, with a replacement cost of $\$ 250$.

If they want to offer a 2 -year extended warranty, what price should they charge so that they'll break even (in other words, so the expected value will be 0 )
a. Make a probability table.
b. Calculate the expected value and answer the question.

