Return tests + go over (I need to collect them back)

Calculate your grade until monday

New material: Section 4.3

Desmos Demo (Project)

www. desmos. com

y = 2x {1< x 23} 

to make a

line segment,

add the domain

# **Zombie Tag!**

### A Zombie is loose in our classroom!

How long until we are all infected?





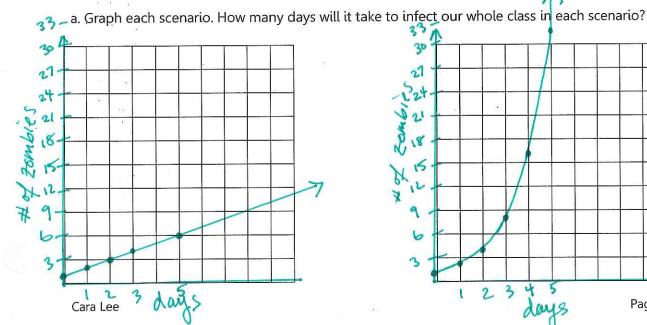
Example 1. Fill in the table for each scenario.

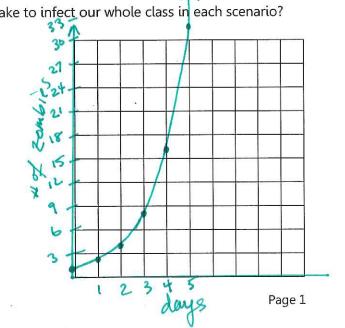
Scenario 1: The initial zombie infects one new person in our class per day. Newly infected zombies cannot infect others.

Days	# of People Infected
Day 0	1 2
Day 1	2 30
Day 2	3
Day 3	4 2
Day 4	5
Day 5	6
Day 6	7 (
Day 7	8
Day 8	9

Scenario 2: The initial zombie and each infected person infect one new person per day.

Days	# of People Infected
Day 0	1 > 2+1=2
Day 1	2 7 4 2=2
Day 2	4 7 7 1 1 2
Day 3	8 / 0 . 1
Day 4	16
Day 5	3 2
Day 6	64
Day 7	128
Day 8	256





b. Write an equation for each scenario:

Scenario 1:

$$y=2^{x}$$
  
 $\pm(x)=2^{x}$ 

Scenario 2:  

$$y = 2^{x}$$

$$2(x) = 2^{x}$$

$$2(x) = 2^{x}$$

$$3 \mid 2^{3} = 8$$

c. How many people would be infected on day 30?

Scenario 1:

$$f(30) = 30 + 1$$
  
= 31 Zombies

Scenario 2:

$$Z(30) = 2^{30}$$
 2 1,073,741,824  
Zombles

d. On which day would the zombie outbreak infect one million people?

Scenario 1:

Scenario 2:

# An exponential function is of the form

$$f(x) = C a^x$$

 $f(x) = Ca^x$  growth rate  $\frac{r}{5}$  b or .05 growth factor 1+r

where

- C is the initial value
- a is the growth factor and a > 0

Consequently, an exponential function is a function that increases or decreases at a constant percent rate. Let's review percent increase and decrease as we work through these examples.

Example 2. You start a new job with an initial salary of \$36,000 per year. Each year thereafter, you receive a 3% raise. Let S(t) be your salary t years after you start your new job.

(a) Write the formula for S(t).

$$C = 36,000$$

$$r=.03$$
  $a=1+.03=1.03$ 

$$S(t) = 36,000(1.03)^{t}$$
  
= 36,000(1.03)<sup>t</sup>

(b) What will your salary be after 10 years?

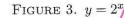
$$S(10) = 36,000 (1.03)^{\circ}$$
  
= \$48,381

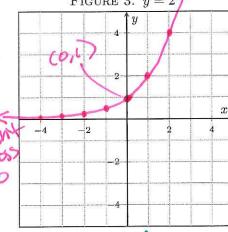
(c) When will your salary reach \$50,000? (Use your graphing calculator to solve this).

**Example 3.** A compost pile has 27 cubic feet of waste and decays at a rate of 10% per month. Let Q(t)be the volume of compost (in cubic feet) t months since decay began. Write the formula for this decreasing exponential function. C= 27 ft3 r=.10

$$a = 1 + \Gamma$$
  
= 1 - .10  
= .90

**Example 4.** Graph of  $y = 2^x$  in Figure 3. Use this to graph the various transformations listed.





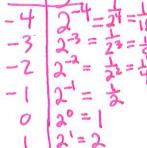


FIGURE 4. 
$$y = 2^x +$$

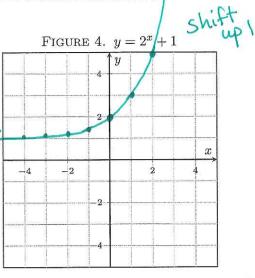
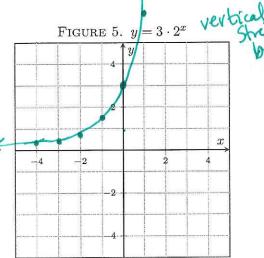
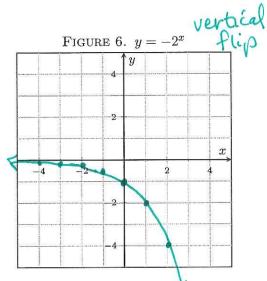
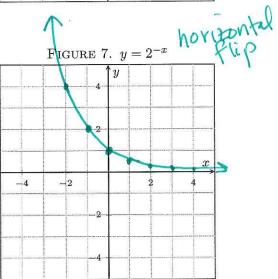
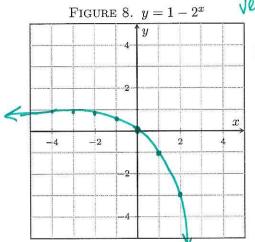


FIGURE 5. 
$$y = 3 \cdot 2^x$$









Example 5. Solve the following equations. List your solution set.

(b) 
$$4^{2x-5} = \frac{1}{16}$$

$$4^{2x-5} = 4^{-2}$$

$$2x-5 = -2$$

$$2x = 32$$

$$x = 32$$

$$x = 32$$

$$x = 32$$

(c) 
$$5^{x^2+8} = 125^{2x}$$

$$5^{x^2+8} = (5^3)^2$$

$$a^{x^2+8} = (5^3)^2$$

$$a^{x^2+8} = 6^{x^2+8}$$

$$x^2+8=6^{x^2+8}$$

$$x^2+8=6^{x^2+8}$$

$$x^2-6^{x^2+8}=0$$

$$(x-2)(x-4)=0$$

$$x-2=0 \text{ or } x-4=0$$

tion set.

(d) 
$$2^{2x-1} = 4$$
 $2^{2x-1} = 4$ 
 $2^{2x-1} = 3$ 
 $2x = 3$ 

(e) 
$$2^{3x-1} = 32$$
  
 $2^{3x-1} = 2^{5}$   
 $3x-1=5$   
 $3x = 6$   
 $x = 2$   
 $2^{2}$ 

(f) 
$$9^{2x} \cdot 27^{x^2} = 3^{-1}$$

$$(3^2)^{2x} \cdot (3^3)^{x} = 3^{-1}$$

$$3^{4x} \cdot 3^{3x^2} = 3^{-1}$$

$$3^{4x+3} \cdot 3^{2x} = 3^{-1}$$

$$3^{2x+4} \cdot 3^{2x} = 3^{-1}$$

A C method 
$$3 \times 2 + 4 \times + 1 = 0$$
  
 $a \cdot c = \frac{3}{3 \cdot 1}$   $3 \times 2 + 3 \times 4 \times + 1 = 0$   
 $3 \times (x+1) + 1(x+1) = 0$   
 $(x+1)(3x+1) = 0$ 

#### WHAT'S "e"?

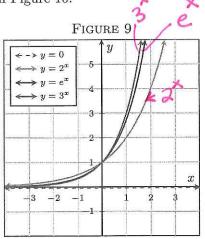
The number e is a number that occurs in nature, and is a frequent base for exponential and logarithmic expressions. It is defined by:

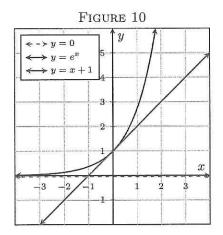
 $e = \lim_{n \to \infty} \left( 1 + \frac{1}{n} \right)^n$ 

It can also be expressed by the following:

$$e = \frac{1}{0!} + \frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \frac{1}{4!} + \frac{1}{5!} + \cdots$$

This number is irrational and is approximated by 2.718281828. The graph of the function given by  $y = e^x$  looks a lot like the graphs of the functions given by  $y = 2^x$  and  $y = 3^x$ , as shown in Figure 9. In calculus, you will study that the special property of e is that the slope of the tangent line at zero is exactly 1, as shown in Figure 10.





Example 6. Solve the following equation.

$$e^{3x} = e^{2-x}$$

$$3x = 2-x$$

$$4x = 2$$

$$4x = 2$$

$$4x = 2$$

$$4x = 2$$

**Simple Interest** 

$$A = P + Prt$$

P = Principal Invested, r = Interest Rate, t=years

**Compound Interest** 

$$A = P\left(1 + \frac{r}{n}\right)^{t/n}$$

n is the number of times the balance is compounded per year

n	Time period	Formula
1	anually	$A = P\left(1 + \frac{r}{1}\right)^{t/1}$
2	bianually	$A = P\left(1 + \frac{r}{2}\right)^{t/2}$
4	quarterly	$A = P\left(1 + \frac{r}{4}\right)^{t/4}$
12	monthly	$A = P\left(1 + \frac{r}{12}\right)^{t/12}$
365	daily	$A = P\left(1 + \frac{r}{356}\right)^{t/365}$
8760	hourly	$A = P \left( 1 + \frac{r}{8760} \right)^{t/8760}$
$\lim_{n\to\infty}$	continuously	$A = Pe^{rt}$

$$e = \lim_{n \to \infty} \left(1 + \frac{1}{n}\right)^n \approx 2.718281828$$

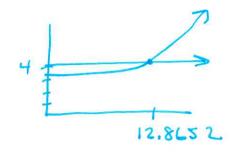
Example 7. In 1990, the population of Oregon was 2.84 million people. In 2010, the population of Oregon was 3.83 million people. Let P(t) be the population of Oregon in millions, where t is the number of years after 2000. This can be modeled by  $P(t) = 3.298e^{0.015t}$ .

(a) According to this model, what will the population be in 2020?

In 2020 the population according the model is 4.45

(b) According to this model, when will the population reach 4 million people? Use your graphing calculator to solve this.

graph 
$$y1 = 4$$
  
 $y2 = 3.298e^{(.015 \times)}$ 



use F5: Intersection (12,8652,4)

2000 + 12.8652

22012.9

In 2012 the population will reach 4 million people according to the model.



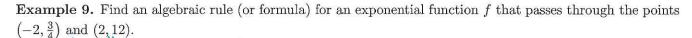
**Example 8.** Find an algebraic rule (or formula) for an exponential function f that passes through the points (-1,8) and (2,1). Also find the algebraic rule (or formula) for a linear function g that passes through the

points (-1,8) and (2,1).

Linear Equation (-1,8) (2,15) constant slope.

M = y2-y1 Slope + a point y-y1=m(x-x.)  $y-1=\frac{7}{3}(x-2)$ y-1=-3x+14  $+1(\frac{3}{3})$ 4 = -73× +5

Exponential Equation y= Cax constant rate (-1, d) (2, 92) 42 = 2ax  $\frac{1}{8} = \frac{a^2}{a^2}$  exponent rules  $a^{2-(-1)} = a^3$  $\frac{1}{8} = a^3$  or  $\frac{1}{8} = a^3$   $(\frac{1}{2})^3 = a^3$   $\frac{1}{2} = a$ = a growth factor FIGURE 11 -2



$$(-2,\frac{3}{4}) \text{ and } (2,12).$$

$$(-2,\frac{3}{4}) \text{ and } (2,12).$$

$$\frac{y_2}{y_1} = \frac{\mathcal{L}a^{\times 2}}{\mathcal{L}a^{\times 1}} \qquad y = C(2)$$

$$12 = C(2)$$

$$13 = C \cdot 4$$

$$15 = a$$

$$2 = a$$

$$2 = a$$

$$3 = C$$

$$16 = a$$

$$2 = a$$

$$3 = C$$

**Example 10.** Find an algebraic rule (or formula) for an exponential function f that passes through the points (1,8) and (3,128).

$$\frac{y_{1}}{y_{1}} = \frac{2a^{2}}{4a^{2}}$$

$$\frac{y_{2}}{y_{1}} = \frac{2a^{2}}{4a^{2}}$$

$$\frac{y_{2}}{y_{1}} = \frac{2a^{2}}{4a^{2}}$$

$$\frac{y_{2}}{y_{2}} = \frac{2a^{2}}{4a^{2}}$$

$$\frac{y_{3}}{y_{4}} = \frac{2a^{2}}{a^{2}}$$

$$\frac{y_{4}}{y_{5}} = \frac{2a^{2}}{a^{2}}$$

$$y_{5} = \frac{2a^{2}}{4a^{2}}$$

$$y_{7} = \frac{2a^{2}}{4a^{2}}$$

**Example 11.** After caffeine is consumed, it leaves the body at a fairly fixed rate. A person consumes 200 mg of caffeine at 8:00am. Four hours later, about 100 milligrams of caffeine are remaining in their bloodstream. Let Q(t) be the number of milligrams of caffeine in the body t hours after consumption.

(a) Write the formula for the function modeling this exponential decay.

$$(0, 200), (4, 100)$$
 $x_1, y_2, y_2$ 

$$\frac{y_2}{y_1} = \frac{(a^{x_2})}{(a^{x_1})}$$

$$\frac{100}{200} = (a^{x_2})$$

$$\frac{100}{2} = (a^{x_2})$$

(b) How much caffeine will still be in the body at 8:00pm?

$$Q(t) = 200(.841)^{t}$$

$$Q(12) = 200(.841)^{12}$$

$$= 260(.841)^{12}$$

$$= 25.037 \text{ mg}$$

